

Thursday, March 7, 2019

4:30–5:20 p.m.

SAS 2102

# The Ramanujan congruences

## for partitions

Heekyoung Hahn

The remarkable **Ramanujan's congruences** for the partition function  $p(n)$  will be presented. Here is Ramanujan's own account:

*"I have proved a number of arithmetic properties of  $p(n)$ ...in particular that*

$$\begin{aligned}p(5n + 4) &\equiv 0 \pmod{5}, \\p(7n + 5) &\equiv 0 \pmod{7}.\end{aligned}$$

*... I have since found another method which enables me to prove all of these properties and a variety of others, of which the most striking is*

$$p(11n + 6) \equiv 0 \pmod{11}.$$

*There are corresponding properties in which the moduli are powers of 5, 7 or 11...It appears that there are no equally simple properties for any moduli involving primes another than these three."*

In this talk, we will discuss Ramanujan's ingenious proofs, his insights and the interesting history behind the account above. This talk should be **accessible to all undergraduates**.

NCSU Society for Undergraduate Mathematics

# SUM Series

## Mathematics and pizza!